

Clearly show all work.

Solve each radical equation:

1.  $\sqrt{x+1} + 3 = 5$   
 $\quad \quad \quad -3 \quad -3$

$\sqrt{x+1} = 2$

$(\sqrt{x+1})^2 = 2^2$

$x+1 = 4$

$x = 3$

$x+1 \geq 0$   
 $x \geq -1$

l.s.  $\sqrt{x+1} + 3$  r.s. 5

$\sqrt{3+1} + 3$

$\sqrt{4} + 3$

$2 + 3$

5 ✓

2.  $x = \sqrt{x+10} + 2$

$x-2 = \sqrt{x+10}$

$(x-2)^2 = (\sqrt{x+10})^2$

$x^2 - 4x + 4 = x + 10$

$x^2 - 5x - 6 = 0$

$(x-6)(x+1) = 0$

$x = 6, -1$

$x+10 \geq 0$   
 $x \geq -10$

l.s. x  
6

r.s.  $\sqrt{x+10} + 2$   
 $\sqrt{6+10} + 2$   
 $\sqrt{16} + 2$   
 $4 + 2$   
6

l.s. x  
-1

r.s.  $\sqrt{x+10} + 2$   
 $\sqrt{-1+10} + 2$   
 $\sqrt{9} + 2$   
 $3 + 2$   
5

✓

x

3.  $(\sqrt{3+w})^2 = (2\sqrt{w-3})^2$

$3+w = 4(w-3)$

$3+w = 4w-12$

$15 = 3w$

$5 = w$

$3+w \geq 0$   
 $w \geq -3$

l.s.  $\sqrt{3+w}$   
 $\sqrt{3+5}$   
 $\sqrt{8}$   
 $2\sqrt{2}$

r.s.  $2\sqrt{w-3}$   
 $2\sqrt{5-3}$   
 $2\sqrt{2}$

✓

$w-3 \geq 0$   
 $w \geq 3$

4.  $\sqrt{4x+5} - \sqrt{2x-1} = 2$

$\sqrt{4x+5} = 2 + \sqrt{2x-1}$

$(\sqrt{4x+5})^2 = (2 + \sqrt{2x-1})^2$

$4x+5 = (2 + \sqrt{2x-1})(2 + \sqrt{2x-1})$

$4x+5 = 4 + 4\sqrt{2x-1} + 2x-1$

$4x+5 = 3 + 2x + 4\sqrt{2x-1}$

$2x+2 = 4\sqrt{2x-1}$

$(2x+2)^2 = (4\sqrt{2x-1})^2$

$4x^2 + 8x + 4 = 16(2x-1)$

$4x^2 + 8x + 4 = 32x - 16$

$4x^2 - 24x + 20 = 0$

$4(x^2 - 6x + 5) = 0$

$4(x-5)(x-1) = 0$

$x = 5, 1$

$4x+5 \geq 0$   
 $x \geq -\frac{5}{4}$

$2x-1 \geq 0$   
 $x \geq \frac{1}{2}$

check

l.s. r.s.  
 $x=5 \checkmark x=1 \checkmark$