

Clearly show all work.

1. State the restriction on the variable in each radical expression:

a) $\sqrt{3x}$

$$3x \geq 0$$

$$x \geq 0$$

b) $\sqrt[3]{5-x}$

No restrictions

c) $\sqrt[4]{3x-1}$

$$3x-1 \geq 0$$

$$3x \geq 1$$

$$x \geq \frac{1}{3}$$

d) $\sqrt{6-2x}$

$$6-2x \geq 0$$

$$-2x \geq -6$$

$$x \leq 3$$

e) $\sqrt{x^2+3}$

No restrictions

2. Simplify:

a) $(3\sqrt{8x})(-2\sqrt{3x})$

$$-6\sqrt{24x^2}$$

$$-6\sqrt{4x^2}\sqrt{6}$$

$$-6(2x)\sqrt{6}$$

$$-12x\sqrt{6}$$

b) $-2\sqrt{5y}(\sqrt{3}-3\sqrt{2y})$

$$-2\sqrt{15y} + 6\sqrt{10y^2}$$

$$-2\sqrt{15y} + 6y\sqrt{10}$$

c) $(4\sqrt{3}+2\sqrt{5})(\sqrt{3}-3\sqrt{5})$

$$4\sqrt{9} - 12\sqrt{15} + 2\sqrt{15} - 6\sqrt{25}$$

$$4(3) - 10\sqrt{15} - 6(5)$$

$$-18 - 10\sqrt{15}$$

d) $(5\sqrt{2}+\sqrt{6})^2$

$$(5\sqrt{2}+\sqrt{6})(5\sqrt{2}+\sqrt{6})$$

$$25\sqrt{4} + 5\sqrt{12} + 5\sqrt{12} + \sqrt{36}$$

$$50 + 10\sqrt{12} + 6$$

$$56 + 10\sqrt{4}\sqrt{3}$$

$$56 + 20\sqrt{3}$$

e) $\frac{6\sqrt{15}^3}{2\sqrt{8}}$

$$2\sqrt{3}$$

f) $\frac{3}{2} \frac{12\sqrt{3}}{8\sqrt{25}}$

$$= \frac{3\sqrt{1}}{2\sqrt{25}}$$

$$= \frac{3}{2(5)}$$

$$= \frac{3}{10}$$

$$\begin{aligned}
 \text{g) } \frac{4\sqrt{5}}{\sqrt{10}} &= \frac{4}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} \\
 &= \frac{4\sqrt{2}}{2} \\
 &= 2\sqrt{2}
 \end{aligned}$$

$$\begin{aligned}
 \text{h) } \frac{2+\sqrt{3}}{3\sqrt{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}} \\
 \frac{2\sqrt{5} + \sqrt{15}}{3\sqrt{25}} \\
 \frac{2\sqrt{5} + \sqrt{15}}{15}
 \end{aligned}$$

$$\begin{aligned}
 \text{i) } \frac{3}{3-\sqrt{2}} \cdot \frac{3+\sqrt{2}}{3+\sqrt{2}} \\
 \frac{9+3\sqrt{2}}{9+3\sqrt{2}-3\sqrt{2}-\sqrt{4}} \\
 \frac{9+3\sqrt{2}}{7}
 \end{aligned}$$

$$\begin{aligned}
 \text{j) } \frac{\sqrt{6}}{2+3\sqrt{3}} \cdot \frac{2-3\sqrt{3}}{2-3\sqrt{3}} \\
 \frac{2\sqrt{6} - 3\sqrt{18}}{4 - 6\sqrt{3} + 6\sqrt{3} - 9\sqrt{9}} \\
 \frac{2\sqrt{6} - 3\sqrt{9}\sqrt{2}}{4 - 27} \\
 \frac{2\sqrt{6} - 9\sqrt{2}}{-23}
 \end{aligned}$$